

QCD Corrections to Squark Production in e^+e^- Annihilation in the MSSM with Complex Parameters

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We discuss the pair production of scalar quarks in e^+e^- annihilation within the MSSM with complex parameters. We calculate the *SUSY*-QCD corrections to the cross section $e^+e^- \rightarrow \tilde{q}_i\tilde{q}_j$ ($i, j = 1, 2$) and show that the effect of the CP phases of these complex parameters on the cross section can be quite strong in a large region of the MSSM parameter space. This could have important implications for squarks searches and the MSSM parameter determination in future collider experiments.

KEY WORDS: MSSM; CP violation.

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1. INTRODUCTION

Supersymmetry is the currently best motivated extension of the Standard Model (SM) of particle physics which allows to stabilize the gauge hierarchy without getting into conflict with electroweak precision data. Among all possible supersymmetric theories, the Minimal Supersymmetric Standard Model (MSSM) occupies a special position. It is not only the simplest, i.e. most economical, potentially realistic supersymmetric field theory, but it also has just the right particle content to allow for the unification of all gauge interactions. The MSSM predicts the existence of scalar partners to all known quarks and leptons. Each fermions has two spin zero partners called sfermions \tilde{f}_L and \tilde{f}_R , one for each chirality eigenstate: the mixing between \tilde{f}_L and \tilde{f}_R is proportional to the corresponding fermion

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mass, and so negligible except for the third generation. In particular, this model gives the possibility for one of the scalar partners of the top quark (\tilde{t}_1) to be lighter than other scalar quarks and also than the top quark (Ellis and Rudaz, 1983).

So far most phenomenological studies on supersymmetric (*SUSY*) particle searches have been performed in the MSSM with real *SUSY* parameters. Studies of the 3rd generation sfermions are particularly interesting because of the effects of the large Yukawa couplings. The lighter sfermion mass eigenstates may be relatively light and they could be thoroughly studied at an e^-e^+ linear collider (Accomando *et al.*, 1998). An analysis of the QCD corrections to scalar quark pair production in e^+e^- annihilation in the MSSM with real parameters was performed in (Arhrib *et al.*, 1995; Eberl *et al.*, 1996).

The assumption that all *SUSY* parameters are real, however, may be too restrictive. The higgsino mass parameter μ , the gaugino masses \tilde{M}_i and the trilinear scalar coupling parameters A_f of the sfermions \tilde{f} may be complex. In the MSSM the complex parameters provide the CP violating phases. Recently, a phenomenological study of τ -sleptons $\tilde{\tau}_{1,2}$ and τ -sneutrinos $\tilde{\nu}_\tau$ has been presented (Bartl *et al.*, 2002), and the effect of the CP phases on the $\tilde{t}_{1,2}$ and $\tilde{b}_{1,2}$ decays has been found (Bartl *et al.*, 2003) in the MSSM with complex parameters. Next, in (Thuy *et al.*, 2004) the one loop vertex correction to the decay width of squark decays into W and Z bosons within the MSSM with complex parameters has been calculated and the numerical results are also performed.

In this article we study the effects of the phases of the complex parameters A_q on the cross sections of the process: $e^+e^- \rightarrow \tilde{q}_i\tilde{q}_j$. We point out that these effects can be quite strong in a large region of the MSSM parameter space. This could have an important impact on the search for squarks and the determination of the MSSM parameters at future colliders. Our present study is an extension of the corresponding one in the MSSM with real parameters in (Arhrib *et al.*, 1995; Eberl *et al.*, 1996).

2. DIAGONALIZATION OF MASS MATRICES

We neglect generation mixing. As pointed out in (Dugan *et al.*, 1985; Christora and Fabbrichesi, 1993) only three terms in the supersymmetric Lagrangian can give rise to CP-violating phases which cannot be rotated away: The superpotential contains a complex coefficient μ in the term bilinear in the Higgs superfields. The soft supersymmetry breaking operators introduce two further complex terms, the gaugino masses \tilde{M}_i and the left- and right-handed squark mixing term A_q . In the MSSM one has two types of scalar quarks (squarks), \tilde{q}_L and \tilde{q}_R , corresponding to the left and right helicity states of a quark. The mass matrix in the basis $(\tilde{q}_L, \tilde{q}_R)$ is given by Ellis and Rudaz (1983).

$$\mathcal{M}_{\tilde{q}}^2 = \begin{pmatrix} m_{\tilde{q}_L}^2 & a_q m_q \\ a_q m_q & m_{\tilde{q}_R}^2 \end{pmatrix} = (\mathcal{R}^{\tilde{q}})^+ \begin{pmatrix} m_{\tilde{q}_1}^2 & 0 \\ 0 & m_{\tilde{q}_2}^2 \end{pmatrix} \mathcal{R}^{\tilde{q}}, \quad (1)$$

with

$$m_{\tilde{q}_L}^2 = \mathcal{M}_{\tilde{Q}}^2 + m_Z^2 \cos 2\beta (I_{3L}^q - e_q s_W^2) + m_q^2, \quad (2)$$

$$m_{\tilde{q}_R}^2 = \mathcal{M}_{\{\tilde{u}, \tilde{D}\}}^2 + e_q m_Z^2 \cos 2\beta s_W^2 + m_q^2, \quad (3)$$

$$a_q = A_q - \mu \{\cot \beta, \tan \beta\}, \quad (4)$$

for {up, down} type squarks, respectively. e_q and I_3^q are the electric charge and the third component of the weak isospin of the squark \tilde{q} , and m_q is the mass of the partner quark. $M_{\tilde{Q}}$, $M_{\tilde{u}}$, and $M_{\tilde{D}}$ are soft *SUSY* breaking masses, and A_q are trilinear couplings.

According to eq. (1) $\mathcal{M}_{\tilde{q}}^2$ is diagonalized by a unitary matrix $\mathcal{R}^{\tilde{q}}$. The weak eigenstates \tilde{q}_L and \tilde{q}_R are thus related to their mass eigenstates \tilde{q}_1 and \tilde{q}_2 by

$$\begin{pmatrix} \tilde{q}_1 \\ \tilde{q}_2 \end{pmatrix} = \mathcal{R}^{\tilde{q}} \begin{pmatrix} \tilde{q}_L \\ \tilde{q}_R \end{pmatrix}, \quad (5)$$

$$\mathcal{R}^{\tilde{q}} = \begin{pmatrix} e^{\frac{i}{2}\varphi_q} \cos \theta_{\tilde{q}} & e^{-\frac{i}{2}\varphi_q} \sin \theta_{\tilde{q}} \\ -e^{\frac{i}{2}\varphi_q} \sin \theta_{\tilde{q}} & e^{-\frac{i}{2}\varphi_q} \cos \theta_{\tilde{q}} \end{pmatrix}, \quad (6)$$

with $\theta_{\tilde{q}}$ is the squark mixing angle and $\varphi_q = \arg(A_q)$. The mass eigenvalues are given by

$$m_{\tilde{q}_{1,2}}^2 = \frac{1}{2} \left(m_{\tilde{q}_L}^2 + m_{\tilde{q}_R}^2 \mp \sqrt{(m_{\tilde{q}_L}^2 - m_{\tilde{q}_R}^2)^2 + 4a_q^2 m_q^2} \right). \quad (7)$$

By convention, we choose \tilde{q}_1 to be the lighter mass eigenstate. For the mixing angle $\theta_{\tilde{q}}$ we require $0 \leq \theta_{\tilde{q}} \leq \pi$. We thus have

$$\cos \theta_{\tilde{q}} = \frac{-|a_q| m_q}{\sqrt{(m_{\tilde{q}_L}^2 - m_{\tilde{q}_1}^2)^2 + a_q^2 m_q^2}}, \quad \sin \theta_{\tilde{q}} = \frac{m_{\tilde{q}_L}^2 - m_{\tilde{q}_1}^2}{\sqrt{(m_{\tilde{q}_L}^2 - m_{\tilde{q}_1}^2)^2 + a_q^2 m_q^2}}. \quad (8)$$

3. THE $\tilde{Q}\tilde{Q}\gamma$ AND $\tilde{Q}\tilde{Q}Z$ COUPLINGS

From the matrix we can find the interaction of a neutral gauge boson $V = \gamma, Z$ with squarks in the general forms

$$\begin{aligned} \mathcal{L}_{\tilde{q}\tilde{q}\gamma} &= i e e_q A_\mu (\tilde{q}_L^* \overleftrightarrow{\partial}^\mu \tilde{q}_L + \tilde{q}_R^* \overleftrightarrow{\partial}^\mu \tilde{q}_R) \\ &= i e e_q A_\mu (\mathcal{R}_{i1}^{\tilde{q}} \mathcal{R}_{j1}^{\tilde{q}} + \mathcal{R}_{i2}^{\tilde{q}} \mathcal{R}_{j2}^{\tilde{q}}) \tilde{q}_j^* \overleftrightarrow{\partial}^\mu \tilde{q}_i \\ &\equiv i e e_q \delta_{ij} \tilde{q}_j^* \overleftrightarrow{\partial}^\mu \tilde{q}_i, \end{aligned} \quad (9)$$

where

$$\delta = \begin{pmatrix} \cos \varphi_q + i \sin \varphi_q \cos 2\theta_{\tilde{q}} & -i \sin \varphi_q \sin 2\theta_{\tilde{q}} \\ -i \sin \varphi_q \sin 2\theta_{\tilde{q}} & \cos \varphi_q - i \sin \varphi_q \cos 2\theta_{\tilde{q}} \end{pmatrix}, \quad (10)$$

and

$$\begin{aligned} \mathcal{L}_{\tilde{q}\tilde{q}Z} &= \frac{ig}{c_w} Z_\mu \left(c_{qL} \tilde{q}_L^* \overleftrightarrow{\partial}^\mu \tilde{q}_L + c_{qR} \tilde{q}_R^* \overleftrightarrow{\partial}^\mu \tilde{q}_R \right) \\ &\equiv \frac{ig}{c_w} Z_\mu C_{ij} \tilde{q}_j^* \overleftrightarrow{\partial}^\mu \tilde{q}_i, \end{aligned} \quad (11)$$

where

$$C = \begin{pmatrix} (I_{3L}^q \cos^2 \theta_{\tilde{q}} - e_q s_W^2) \cos \varphi_q & -\frac{1}{2} I_{3L}^q \sin 2\theta_{\tilde{q}} \cos \varphi_q \\ +i(I_{3L}^q \cos^2 \theta_{\tilde{q}} - e_q s_W^2 \cos 2\theta_{\tilde{q}}) \sin \varphi_q & +i(e_q s_W^2 - \frac{1}{2} I_{3L}^q) \sin 2\theta_{\tilde{q}} \sin \varphi_q \\ -\frac{1}{2} I_{3L}^q \sin 2\theta_{\tilde{q}} \cos \varphi_q & (I_{3L}^q \sin^2 \theta_{\tilde{q}} - e_q s_W^2) \cos \varphi_q \\ +i(e_q s_W^2 - \frac{1}{2} I_{3L}^q) \sin 2\theta_{\tilde{q}} \sin \varphi_q & +i(I_{3L}^q \sin^2 \theta_{\tilde{q}} + e_q s_W^2 \cos 2\theta_{\tilde{q}}) \sin \varphi_q \end{pmatrix}. \quad (12)$$

We obtain the corresponding Feynman rules from

$$\tilde{q}_j^* \overleftrightarrow{\partial}^\mu \tilde{q}_i = i(k_i + k_j)^\mu,$$

where k_i and k_j are the four-momenta of \tilde{q}_i and \tilde{q}_j in direction of the charge flow. The coupling between a gauge boson V and two squarks \tilde{q}_i and \tilde{q}_j with $i, j = 1, 2$ is given by (the directions of the momenta are shown in Fig. 1):

$$\Gamma_{\tilde{q}_i \tilde{q}_j \gamma}^\mu = -ie e_q (\bar{k} + k)^\mu \delta_{ij}, \quad (13)$$

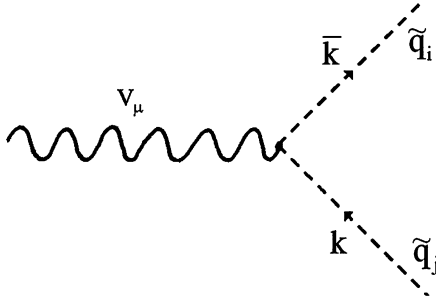


Fig. 1. The $V\tilde{q}_i\tilde{q}_j$ vertex ($i, j = 1, 2$).

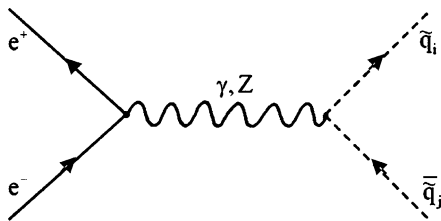


Fig. 2. Feynman diagrams for the process $e^+e^- \rightarrow \bar{q}_i \bar{q}_j$ ($i, j = 1, 2$).

$$\Gamma_{\bar{q}_i \bar{q}_j Z}^\mu = -\frac{ig}{c_W} (\bar{k} + k)^\mu c_{ij}. \quad (14)$$

4. TREE LEVEL FORMULAE

In this section we discuss the pair production of squarks in e^+e^- collisions. The process $e^+e^- \rightarrow \bar{q}_i \bar{q}_j$ proceeds via γ and Z exchange, see Fig. 2.

Using the results just obtained we get the cross section at tree level for unpolarized beams:

$$\sigma^0 = \frac{\sqrt{2}\pi\alpha^2\lambda_{ij}^{3/2}}{s} \left[e_q^2 |\delta_{ij}|^2 - \frac{e_q v_e}{4c_W^2 s_W^2} (c_{ij} \delta_{ij}^+ + c_{ij}^+ \delta_{ij}) \cdot D_{\gamma Z} + \frac{v_e^2 + a_e^2}{16c_W^4 s_W^4} |c_{ij}|^2 D_{ZZ} \right], \quad (15)$$

where s is the *c.m.* energy squared, $\lambda_{ij} = [(s - m_i^2 - m_j^2)^2 - 4m_i^2 m_j^2]$, e_q is the charge of the squarks ($e_t = 2/3$, $e_b = -1/3$) in the units of e ($= \sqrt{4\pi\alpha}$), $a_e = -1$, $v_e = -1 + 4s_w^2$ (with $s_w \equiv \sin\theta_w$, $c_w \equiv \cos\theta_w$), and

$$D_{\gamma Z} = \frac{s(s - M_Z^2)}{(s - m_Z^2)^2 + m_Z^2 \Gamma_Z^2}, \quad (16)$$

$$D_{ZZ} = \frac{s^2}{(s - m_Z^2)^2 + m_Z^2 \Gamma_Z^2}. \quad (17)$$

5. SUSY—QCD CORRECTIONS

The *SUSY* QCD corrected cross section, corresponding to Fig. 3 can be written as

$$\sigma = \sigma^0 + \delta\sigma^0. \quad (18)$$

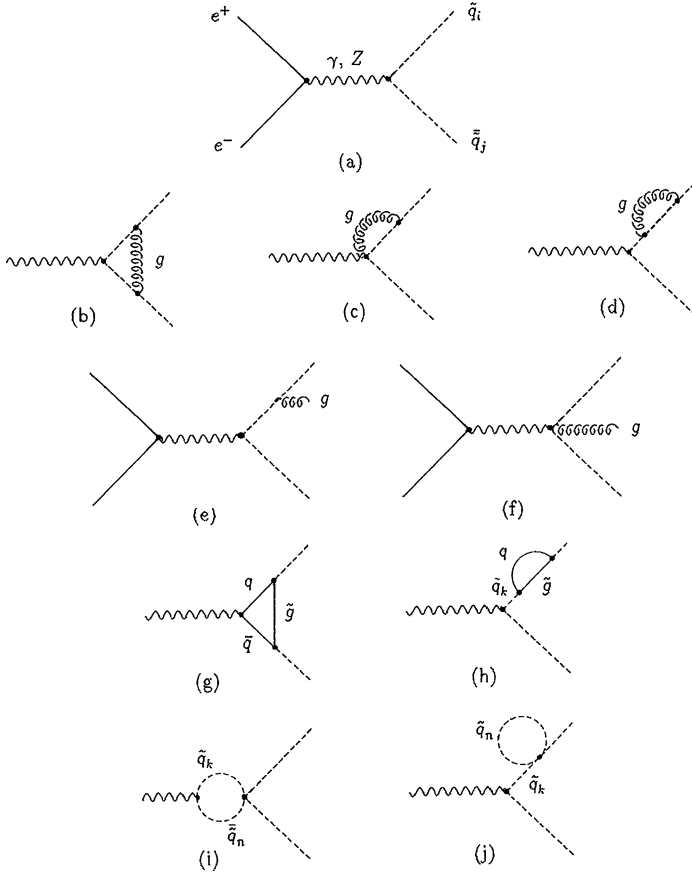


Fig. 3. Feynman diagrams for the lowest order SUSY-QCD corrections to $e^+e^- \rightarrow \tilde{q}_i\bar{\tilde{q}}_j$.

Here

$$\delta\sigma^0 = \frac{\pi\alpha^2\lambda_{ij}^{3/2}}{s} \frac{\alpha_s}{3\pi} \text{Re}\{\delta A_1 + \delta A_2 + \delta A_3 + \delta A_4 + \delta A_5\}, \quad (19)$$

with

$$\begin{aligned} \delta A_1 = & \{i\delta_{ii}\delta_{jj}2[B_1(m_i^2, m_g^2, m_i^2) + B_0(m_i^2, m_g^2, m_i^2) + B_1(m_j^2, m_g^2, m_j^2) \\ & + B_0(m_j^2, m_g^2, m_j^2) - (2s - 2m_i^2 - 2m_j^2 - m_g^2)(C_{11} + C_0)] \\ & + 8\delta_{ii}[B_1(m_i^2, m_g^2, m_i^2) + 2B_0(m_i^2, m_g^2, m_i^2)] \\ & - i\delta_{ii}\delta_{ii}[A(m_i^2) - m_g^2 B_0(m_i^2, m_g^2, m_i^2)] \end{aligned}$$

$$\begin{aligned}
& + 4i \sum_{k=1}^2 [(A(m_q^2) - m_g^2 B_0(m_i^2, m_{\bar{g}}^2, m_q^2)) \delta_{ki} \\
& - (m_{\bar{g}} \delta_{ki} - m_q m_{\bar{g}} C_{ki}) B_0(m_i^2, m_{\bar{g}}^2, m_q^2) + 2S_{ik} S_{ik} A(m_k^2)] \}^+ \cdot \\
& \left[e_q^2 |\delta_{ij}|^2 + \frac{(v_e^2 + a_e^2) |C_{ij}|^2}{16C_W^4 S_W^4} D_{ZZ} - \frac{e_q v_e [C_{ij} \delta_{ij}^+ + C_{ij}^+ \delta_{ij}]}{4C_W^2 S_W^2} D_{\gamma Z} \right], \quad (20)
\end{aligned}$$

$$\begin{aligned}
\delta A_2 = & 2 \{ \delta_{ij} [(2m_{\bar{g}}^2 + m_i^2 + m_j^2 + m_{q^\alpha}^2 + m_{q^\beta}^2)(C'_{11} + C'_0) - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\beta}^2) \\
& - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\alpha}^2) + (m_{q^\alpha}^2 + m_{q^\beta}^2 + 0.5s \\
& + 0.5m_i^2 + 0.5m_j^2 + 2m_{q^\alpha} m_{q^\beta}) \cdot C'_{11}] \\
& - 2m_{\bar{g}}(m_{q^\beta} + m_{q^\alpha}) \cdot E_{ij}(C'_{11} + C'_0) \}^+ (e_q^2 \delta_{ij}), \quad (21)
\end{aligned}$$

$$\begin{aligned}
\delta A_3 = & 2 \{ -\delta_{ijRL} [(2m_{\bar{g}}^2 + m_i^2 + m_j^2 + m_{q^\alpha}^2 + m_{q^\beta}^2)(C'_{11} + C'_0) - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\beta}^2) \\
& - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\alpha}^2) + (m_{q^\alpha}^2 + m_{q^\beta}^2 + 0.5s + 0.5m_i^2 + 0.5m_j^2) \cdot C'_{11}] \\
& + 2m_{\bar{g}}(m_{q^\beta} C_{ijRL} + m_{q^\alpha} C_{ijLR})(C'_{11} + C'_0) - 2m_{q^\alpha} m_{q^\beta} C_{ij} C'_{11} \} \\
& + \frac{e_q v_e \delta_{ij}}{2C_W^2 S_W^2} D_{\gamma Z}, \quad (22)
\end{aligned}$$

$$\begin{aligned}
\delta A_4 = & 2E_{ij} \{ \delta_{ij} [(2m_{\bar{g}}^2 + m_i^2 + m_j^2 + m_{q^\alpha}^2 + m_{q^\beta}^2)(C'_{11} + C'_0) - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\beta}^2) \\
& - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\alpha}^2) + (m_{q^\alpha}^2 + m_{q^\beta}^2 + 0.5s \\
& + 0.5m_i^2 + 0.5m_j^2 + 2m_{q^\alpha} m_{q^\beta}) \cdot C'_{11}] \\
& - 2m_{\bar{g}}(m_{q^\beta} + m_{q^\alpha}) \cdot E_{ij}(C'_{11} + C'_0) \} + \frac{e_q v_e \delta_{ij}}{2C_W^2 S_W^2} D_{\gamma Z}, \quad (23)
\end{aligned}$$

$$\begin{aligned}
\delta A_5 = & 2E_{ij} \{ \delta_{ijRL} [(2m_{\bar{g}}^2 + m_i^2 + m_j^2 + m_{q^\alpha}^2 + m_{q^\beta}^2)(C'_{11} + C'_0) - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\beta}^2) \\
& - B_0(m_i^2, m_{\bar{g}}^2, m_{q^\alpha}^2) + (m_{q^\alpha}^2 + m_{q^\beta}^2 + 0.5s + 0.5m_i^2 + 0.5m_j^2) \cdot C'_{11}] \\
& + 2m_{\bar{g}}(m_{q^\beta} C_{ijRL} + m_{q^\alpha} C_{ijLR})(C'_{11} + C'_0) - 2m_{q^\alpha} m_{q^\beta} C_{ij} C'_{11} \} \\
& + \frac{v_e^2 + a_e^2}{16C_W^4 S_W^4} D_{ZZ}. \quad (24)
\end{aligned}$$

and

$$\begin{aligned}
\delta_{ijRL} &= C_{qR} \mathcal{R}_{i1}^{\tilde{q}} \mathcal{R}_{j1}^{\tilde{q}} + C_{qL} \mathcal{R}_{i2}^{\tilde{q}} \mathcal{R}_{j2}^{\tilde{q}}, \\
C_{ijLR} &= C_{qL} \mathcal{R}_{i1}^{\tilde{q}} \mathcal{R}_{j2}^{\tilde{q}} + C_{qR} \mathcal{R}_{i2}^{\tilde{q}} \mathcal{R}_{j1}^{\tilde{q}}, \\
C_{ijRL} &= C_{qR} \mathcal{R}_{i1}^{\tilde{q}} \mathcal{R}_{j2}^{\tilde{q}} + C_{qL} \mathcal{R}_{i2}^{\tilde{q}} \mathcal{R}_{j1}^{\tilde{q}}, \\
E_{ij} &= \mathcal{R}_{i1}^{\tilde{q}} \mathcal{R}_{j2}^{\tilde{q}} + \mathcal{R}_{i2}^{\tilde{q}} \mathcal{R}_{j1}^{\tilde{q}}, \\
S_{ij} &= \mathcal{R}_{i1}^{\tilde{q}} \mathcal{R}_{j1}^{\tilde{q}} - \mathcal{R}_{i2}^{\tilde{q}} \mathcal{R}_{j2}^{\tilde{q}}, \\
C_0 &= C_0(m_i^2, s, m_j^2, m_{\tilde{g}}^2, m_i^2, m_j^2), \\
C_{11} &= C_{11}(m_i^2, s, m_j^2, m_{\tilde{g}}^2, m_i^2, m_j^2), \\
C'_0 &= C'_0(m_i^2, s, m_j^2, m_{\tilde{g}}^2, m_{q^\alpha}^2, m_{q^\beta}^2), \\
C'_{11} &= C'_{11}(m_i^2, s, m_j^2, m_{\tilde{g}}^2, m_{q^\alpha}^2, m_{q^\beta}^2).
\end{aligned}$$

We now turn to the numerical analysis of the *SUSY*—QCD corrections.

In Fig. 4 we show the $\phi \equiv \varphi_q$ dependence of the σ_R^0/σ_C^0 , $\delta\sigma_R^0/\delta\sigma_C^0$ and $\delta\sigma_C/\sigma_C^0$, with *R* and *C* indices corresponding to the cases of real and complex parameters respectively. The input parameters are: $\sqrt{s} = 1000$ GeV, $m_{\tilde{t}_1} = 400$ GeV, $m_{\tilde{t}_2} = 600$ GeV, $m_{\tilde{b}_1} = 400$ GeV, $m_{\tilde{b}_2} = 450$ GeV, $m_{\tilde{g}} = 600$ GeV, $|\cos\theta_t| = |\cos\theta_b| = 0.5$. Here we concentrate on the range of the complex phase φ_q of the A_q -parameter, it must be less than of order 10^{-2} – 10^{-3} to avoid generating electric dipole moments for the neutron, electron, and atom in conflict with observed data (Review of Particle Physics, 1998). In the range of ϕ shown, σ_R^0/σ_C^0

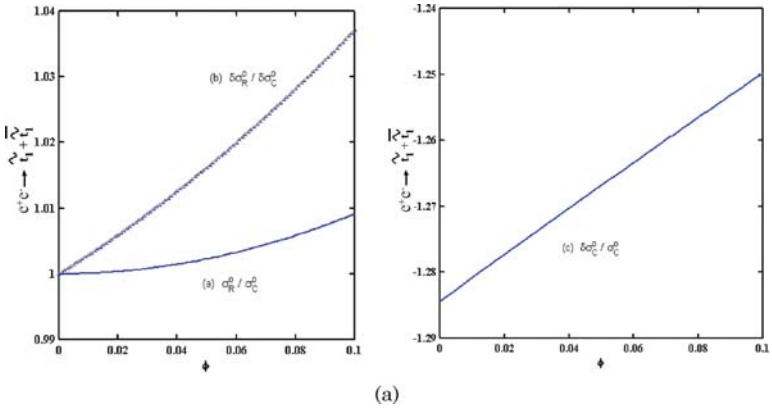


Fig. 4. Cross sections and their corrections of (a) $e^+e^- \rightarrow \tilde{t}_1\tilde{t}_1$, (b) $e^+e^- \rightarrow \tilde{t}_2\tilde{t}_2$, (c) $e^+e^- \rightarrow \tilde{b}_1\tilde{b}_1$, and (d) $e^+e^- \rightarrow \tilde{b}_2\tilde{b}_2$ as functions of Φ , for $\cos\theta_t = \cos\theta_b = 0.5$; $\sqrt{s} = 1000$ GeV, $m_{\tilde{t}_1} = m_{\tilde{b}_1} = 400$ GeV, $m_{\tilde{t}_2} = m_{\tilde{g}} = 600$ GeV, $m_{\tilde{b}_2} = 450$ GeV.

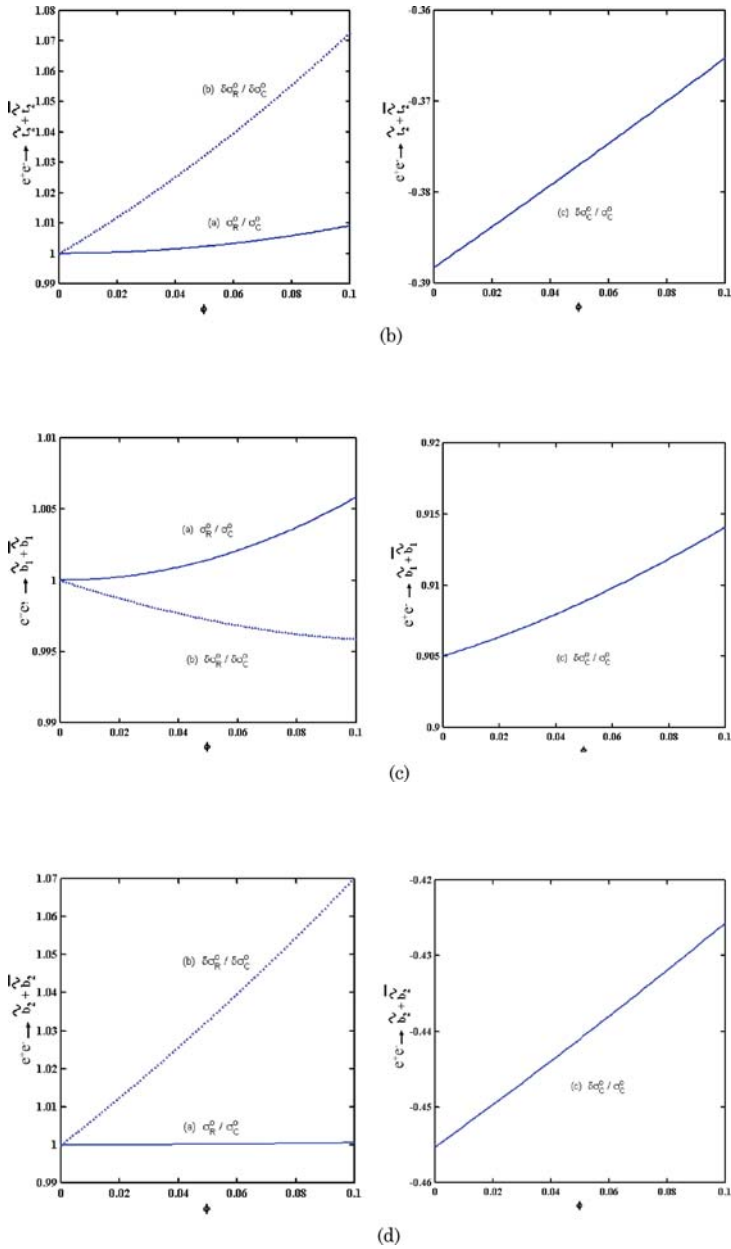


Fig. 4. Continued.

varies from 100% to 99% in cases of $\tilde{t}_1\tilde{t}_1$ or $\tilde{t}_2\tilde{t}_2$ productions (Fig. 4(a) and (b)) and is about from 100% to 99.5% and 100% for $\tilde{b}_1\tilde{b}_1$ and $\tilde{b}_2\tilde{b}_2$ productions (Fig. 4(c) and (d)).

The corrections $\delta\sigma_C^0/\sigma_C^0$ are from -28.4% to -25% , from -38.8% to -36.5% , and from -45.5% to -42.5% for the $\tilde{t}_1\tilde{t}_1$, $\tilde{t}_2\tilde{t}_2$, $\tilde{b}_1\tilde{b}_1$ and $\tilde{b}_2\tilde{b}_2$ productions, respectively. We have also computed $\delta\sigma_R^0/\delta\sigma_C^0$. It is about from 99.5% to 96.5%, from 99.5% to 93%, from 100% to 99.5%, and from 100% to 93%, for the above mentioned processes, respectively.

6. CONCLUSIONS

In this paper, we have calculated the QCD radiative corrections to the production of squarks in e^+e^- collisions within the MSSM with complex parameters. In particular, we focus on the CP phase dependence of the production cross sections for $e^+e^- \rightarrow \tilde{q}_i\tilde{q}_j$. From numerical results we have found that the effects of the phases on the cross sections can be quite significant in a large region of the MSSM parameter space. This could have important implications for \tilde{t}_i and \tilde{b}_i searches at future colliders and the determination of the underlying MSSM parameters.

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